

Fluctuations near the liquid-gas and chiral phase transitions

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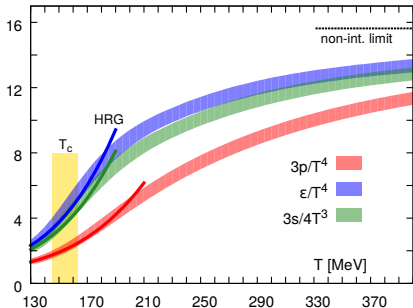
MM, K. Redlich, C. Sasaki, Phys.Rev.D 103 (2021) 5, 054035

MM, K. Redlich, C. Sasaki, Phys.Rev.D 107 (2023) 5, 054046

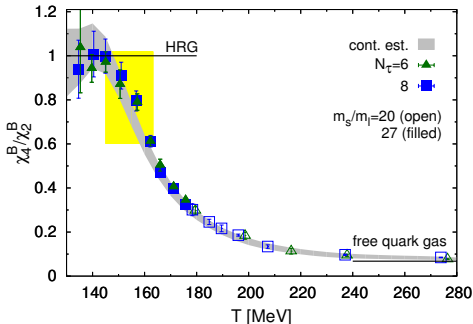
Exploring Quark-Gluon Plasma through soft and hard probes
Belgrade, 30.05.2023



Hadron Resonance Gas vs Lattice QCD

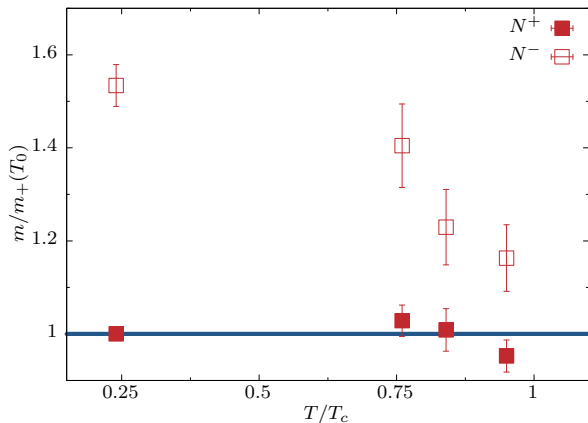


HotQCD, PRD (2014)



HotQCD, PRD (2017)

- Pressure in the HRG: $P^{\text{HRG}}(T, \mu_B, \mu_S, \mu_Q) = \sum_{i \in \text{had}} P^{\text{ideal}}(T, \mu_i; m_i)$
- HRG describes well LQCD equation of state and some fluctuations up to $\simeq T_c$
- Taylor expansion of LQCD Pressure: $P = \sum_{k=0}^{\infty} \left(\frac{\mu_B}{T}\right)^k \frac{\chi_k^B}{k!}$, where $\chi_k^B = \frac{\partial^k P}{\partial (\mu_B/T)^k}$
- Kurtosis: $\frac{\chi_4^B}{\chi_2^B} \sim B^2$: breakdown around $T_c \rightarrow$ changeover to QGP

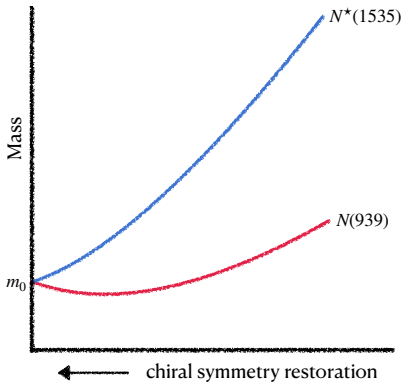


- imprint of chiral symmetry restoration in the baryonic sector
- general tendency: N^+ - const; N^- - dramatic drop toward chiral crossover
- chiral partners N^\pm stay massive around T_c

Parity Doubling in SU(2) Chiral Models: Parity Doublet Model

Model a'la DeTar, Kunihiro PRD 39 (1989) $\longrightarrow \mathcal{L}_{\text{mass}} = m_0(\bar{\psi}_1 \gamma_5 \psi_2 - \psi_2 \gamma_5 \psi_1)$

$$M_{\pm} = \sqrt{4m_0^2 + \alpha^2 \sigma^2} \mp \beta \sigma \xrightarrow{\sigma \rightarrow 0} m_0$$



Chiral symmetry restoration



$$M_- - M_+ = \beta \sigma$$

- Repulsive interactions \rightarrow exchange of ω
- Mean field approximation for chiral criticality

In-medium Hadron Resonance Gas vs Lattice QCD

- parity doubling \rightarrow agreement with LQCD

Aarts *et al* (2018)

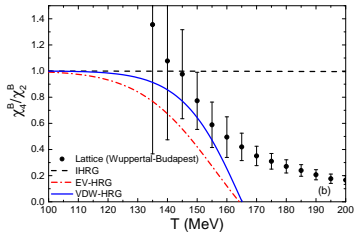
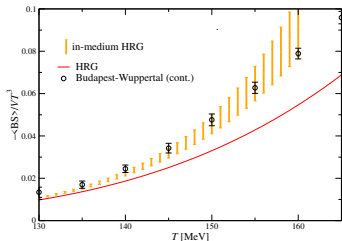
- mass shift \rightarrow agreement is accidental

Morita *et al* (2018)

- excluded volume \rightarrow agreement with LQCD

- deviations from HRG \rightarrow repulsive int.

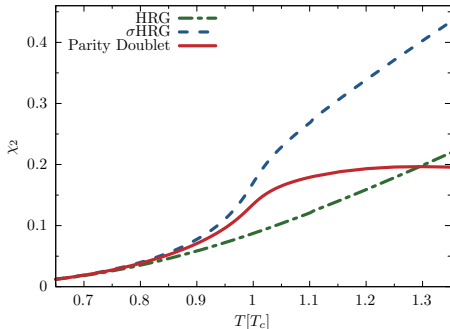
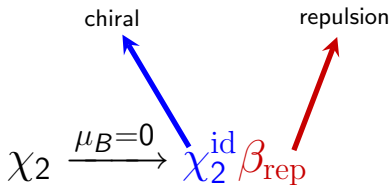
Vovchenko *et al* (2017)



To what extent the behavior is due to chiral criticality and repulsive interactions?

Fluctuations and In-medium Effects in $\sigma - \omega$ Models

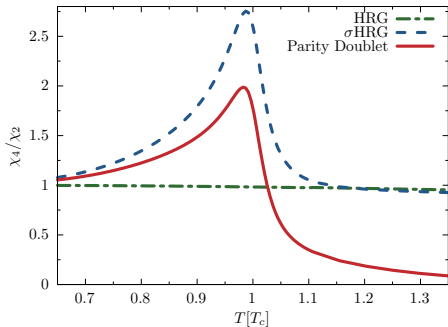
Susceptibility of the net-baryon number: $\chi_n = T^{n-4} \frac{\partial^{n-1} n_B(T, \mu_B, \sigma, \omega)}{\partial \mu_B^{n-1}} \Big|_T$



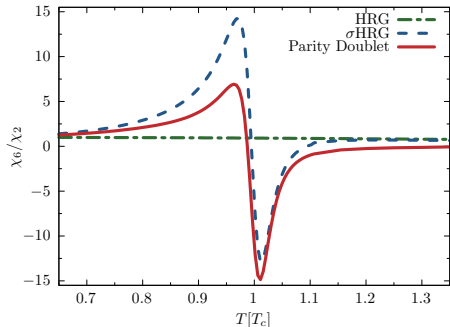
- HRG - non-critical baseline
- HRG $\xrightarrow{+chiral}$ σ HRG $\xrightarrow{+repulsion}$ Parity Doublet
- Qualitative differences in $\chi_2 \rightarrow$ repulsive interactions: $\chi_2 = \chi_2^{\text{id}} \beta_{\text{rep}}$

Ratios of higher-order cumulants: (hyper) kurtosis

interactions \rightarrow strong deviations from the HRG baseline in $\frac{\chi_4}{\chi_2}$ and $\frac{\chi_6}{\chi_2}$

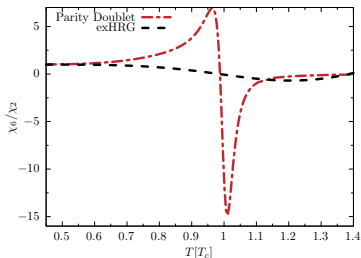


- structure dictated by chiral symmetry
- no chiral-critical behavior encoded in β



- χ_4/χ_2 and χ_6/χ_2 suppressed by repulsion, but qualitative structure the same

Comparison with excluded volume HRG



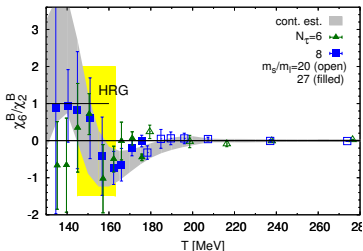
Excluded Volume HRG

$$P^{\text{ev}}(T, \mu) = P^{\text{id}}(T, \mu - v_0 P^{\text{ev}}(T, \mu))$$

Fluctuations no longer skellam:

$$\text{kurtosis} \quad \frac{\chi_4^{\text{ev}}}{\chi_2^{\text{ev}}} \simeq 1 - 12v_0\phi(T)$$

$$\text{hyperkurtosis} \quad \frac{\chi_6^{\text{ev}}}{\chi_2^{\text{ev}}} \simeq 1 - 60v_0\phi(T)$$



- qualitatively different structure of the ratios
- χ_6/χ_2 - fails to capture the characteristic properties

compare with Borsanyi et al (2018); Bazavov et al (2020)

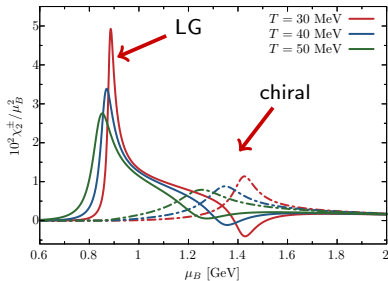
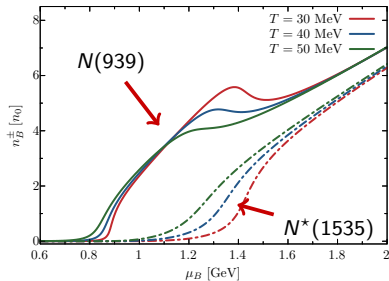
consistent framework with **chiral effects** and repulsive interactions needed

Fluctuations of Chiral Partners at Finite Density

$$n_B = n_B^+ + n_B^- \quad \chi_2 = \chi_2^+ + \chi_2^-$$

N(939) N*(1535)
↙ ↘ ↙ ↘

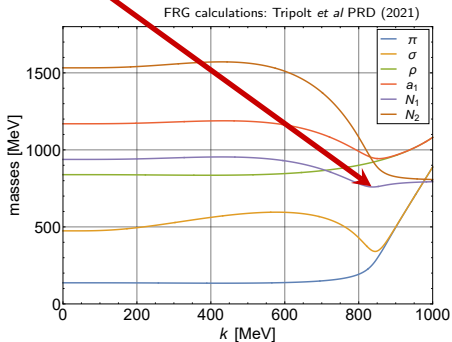
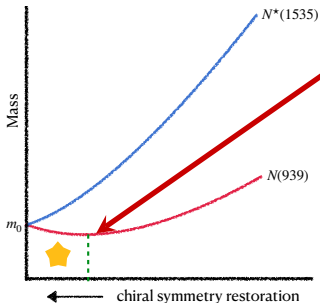
$$\chi_2^\pm = \left. \frac{\partial n_B^\pm}{\partial \mu_B} \right|_T = \frac{\partial n_B^\pm}{\partial \mu_B} + \frac{\partial n_B^\pm}{\partial m_\pm} \frac{\partial m_\pm}{\partial \sigma} \frac{\partial \sigma}{\partial \mu_B} + \frac{\partial n_B^\pm}{\partial \omega} \frac{\partial \omega}{\partial \mu_B}$$



- Critical mode couples to $N(939)$ at liquid-gas phase transition
- Critical mode couples to $N(939)$ and $N^*(1535)$ at chiral phase transition
- χ_2^+ becomes negative at small T

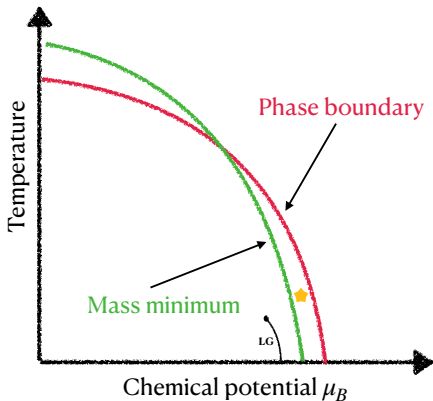
Chiral Critical Mode and Behavior of Nucleon Mass

$$\chi_2^{\pm, \text{crit}} \sim \frac{\partial n_B^{\pm}}{\partial m_{\pm}} \frac{\partial m_{\pm}}{\partial \sigma} \frac{\partial \sigma}{\partial \mu_B}$$



- χ_2^{\pm} diverge with the same critical exp. at CP
- Negativity of χ_2^+ from the restoration of chiral symmetry

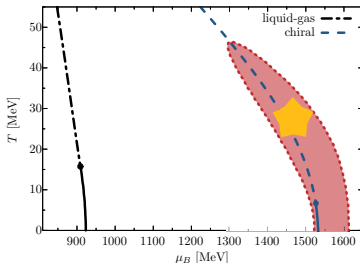
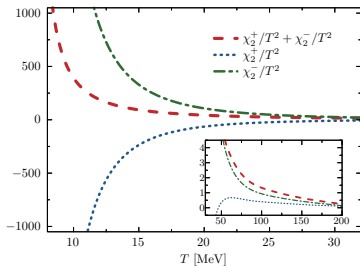
Approaching Critical Point at Phase Boundary



NET-PROTON AS PROXY FOR NET-BARYON



COMMON LORE NOT NECESSARILY CORRECT

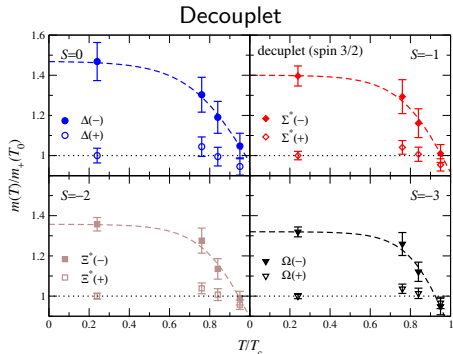
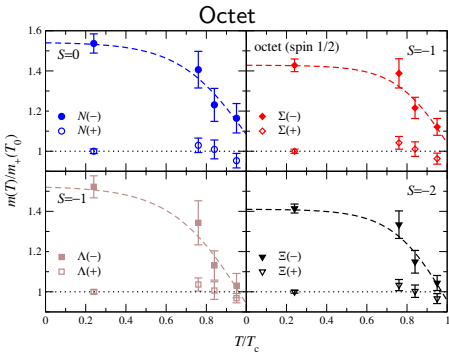


Summary

dominance of chiral criticality at phase boundary

net-proton \leftrightarrow net-baryon not necessarily correct

Thank You



Different decomposition

$$\chi_2^\pm = \frac{\frac{\partial n_B^\pm}{\partial \mu_B} + \chi_2^{\pm, \text{crit}}}{1 + g_\omega \frac{\partial n_B^\pm}{\partial \mu_B}}$$