

# Constraining $\eta/s$ through high- $p_{\perp}$ tomography

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**ExploreQGP**

30 May 2023



**European Research Council**  
Established by the European Commission

# Outline

- Introduction
- $\eta/s$  of the medium : Soft-to-hard boundary
- High- $p_{\perp}$  energy loss: Generalized DREENA-A
- Phenomenological approach to constrain  $\eta/s$
- Theoretical approach to evaluate  $\eta/s$
- Conclusion

# Introduction

- Low- $p_{\perp}$  observables are used to explore the bulk properties of the QGP created in heavy-ion collisions.
- High- $p_{\perp}$  probes also become powerful tomography tools; Sensitive to global QGP features, e.g., different temperature profiles or initial conditions.
- The near perfect fluidity of QGP has been investigated extensively in heavy-ion collision experiments.
- $\eta/s$  is well constrained by Bayesian analysis in low- $p_{\perp}$  sector in the temperature range  $T_c \lesssim T \lesssim 1.5T_c$  and weakly constrained at larger temperatures.
- We try to put constraints on  $\eta/s$  by analyzing high- $p_{\perp}$  observables using the generalized DREENA-A.

# $\eta/s$ of the medium : Soft-to-hard boundary

- QGP is expected to behave as weakly interacting gas: Weakly coupled
- Fluid dynamics predicts the  $\eta/s$  to be very low: Strongly coupled
- QGP may behave as perfect fluid near  $T_c$  (soft regime) and  $\eta/s$  may increase at high temperature (hard regime).
- Testing the soft-to-hard hypothesis is difficult: Anisotropy is weakly affected by the  $\eta/s$  at high temperature.
- High- $p_{\perp}$  data/theory can serve as complementary tool.

# High- $p_{\perp}$ energy loss : Generalized DREENA-A

- **Dynamical Radiative and Elastic ENergy loss Approach**

- Based on finite temperature field theory and generalized HTL approach

- M. Djordjevic, PRC 74, 064907, (2006) ; PRC 80, 064909 (2009), M. Djordjevic and U. Heinz, PRL 101, 022302

- Finite size dynamical QCD medium is considered

- Takes into account both radiative and collisional energy losses

- Generalized to the case of magnetic mass and running coupling

- No fitting parameter in the theory

- Takes arbitrary temperature profile as input.

- D. Zigic, I. Salom, J. Auvinen, P. Huovinen, M. Djordjevic Front.in Phys. 10 (2022) 957019

- Optimized to incorporate any arbitrary event-by-event fluctuating temperature profile.

- D. Zigic, J. Auvinen, I. Salom, M. Djordjevic, P. Huovinen Phys.Rev.C 106 (2022) 4, 044909

- DREENA-A is available on <http://github.com/DusanZigic/DREENA-A> (Details in talk by Dusan Zigic, next session)

# Phenomenological approach

- Three different  $(\eta/s)(T)$  parametrizations have been considered.
- Parameters are adjusted to reproduce low- $p_{\perp}$  data.
- Temperature profile is generated for each case.
- High- $p_{\perp}$  predictions found using generalized DREENA-A.
- Compared with high- $p_{\perp}$  data.

# Modeling the bulk evolution

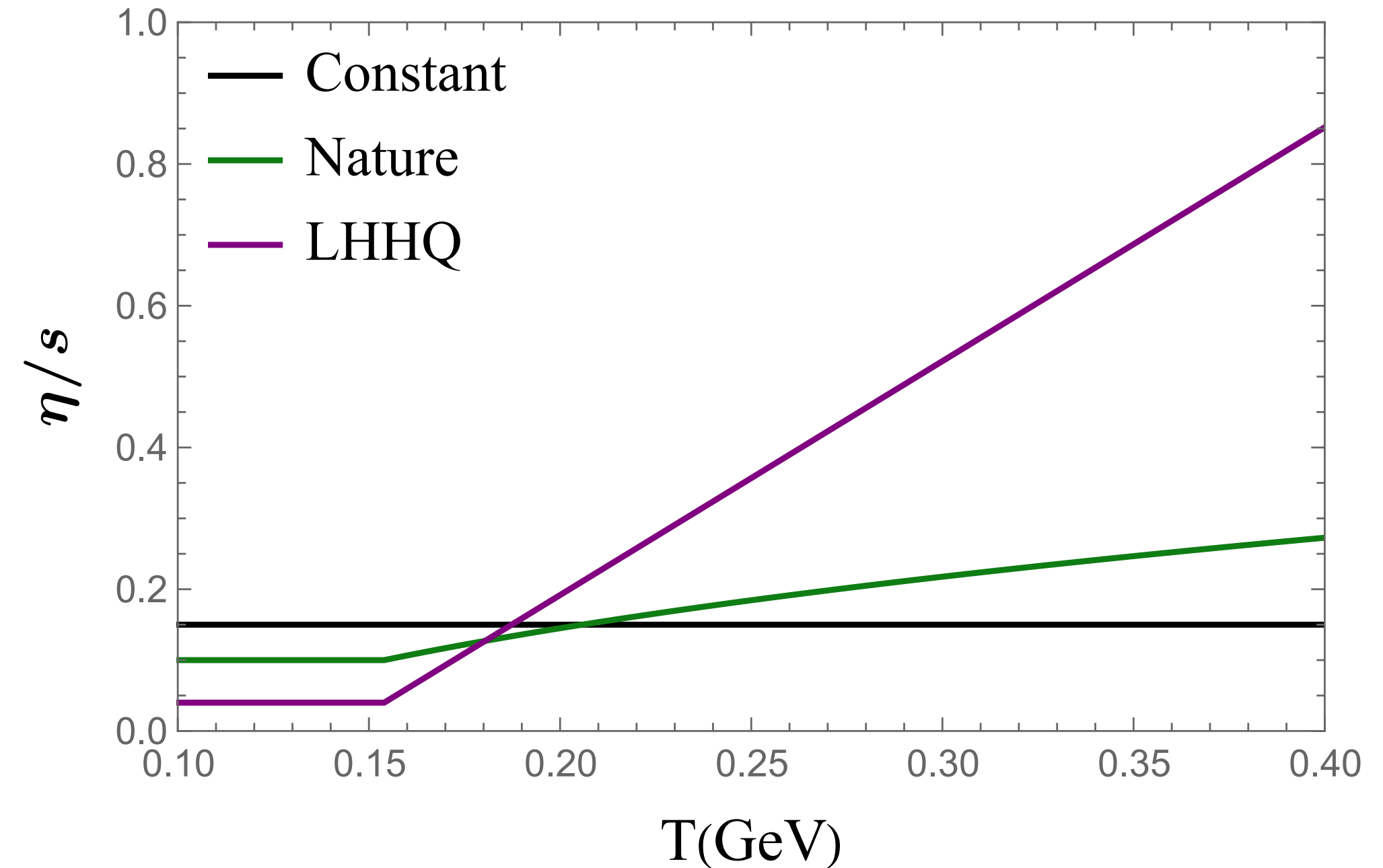
- Initial entropy profiles are generated using TRENTo model.
- $10^4$  events for Pb+Pb ( $\sqrt{s} = 5.02$  TeV) and Au+Au ( $\sqrt{s} = 200$  GeV) collisions.
- Events are sorted in centrality classes.
- Initial free streaming is not preferred by high- $p_{\perp}$  data.  
S. Stojku, J. Auvinen, M. Djordjevic, P. Huovinen and M. Djordjevic, Phys. Rev. C 105 (2022) 2, L021901
- Onset time for hydrodynamics:  $\tau_0 = 1fm$ .  
S. Stojku, J. Auvinen, M. Djordjevic, P. Huovinen and M. Djordjevic, Phys. Rev. C 105 (2022) 2, L021901
- (2+1)-dimensional fluid dynamical model (VISHNew) used to simulate the medium evolution.

# Temperature dependence of $\eta/s$

$$(\eta/s)(T) = \begin{cases} (\eta/s)_{\min}, & T < T_c, \\ (\eta/s)_{\min} + (\eta/s)_{\text{slope}}(T - T_c)\frac{T}{T_c}^{(\eta/s)_{\text{crv}}}, & T > T_c \end{cases}$$

Nature: Nature Phys. 15, no. 11, 1113-1117 (2019)

LHHQ: Phys. Rev. Lett. 106, 212302 (2011)

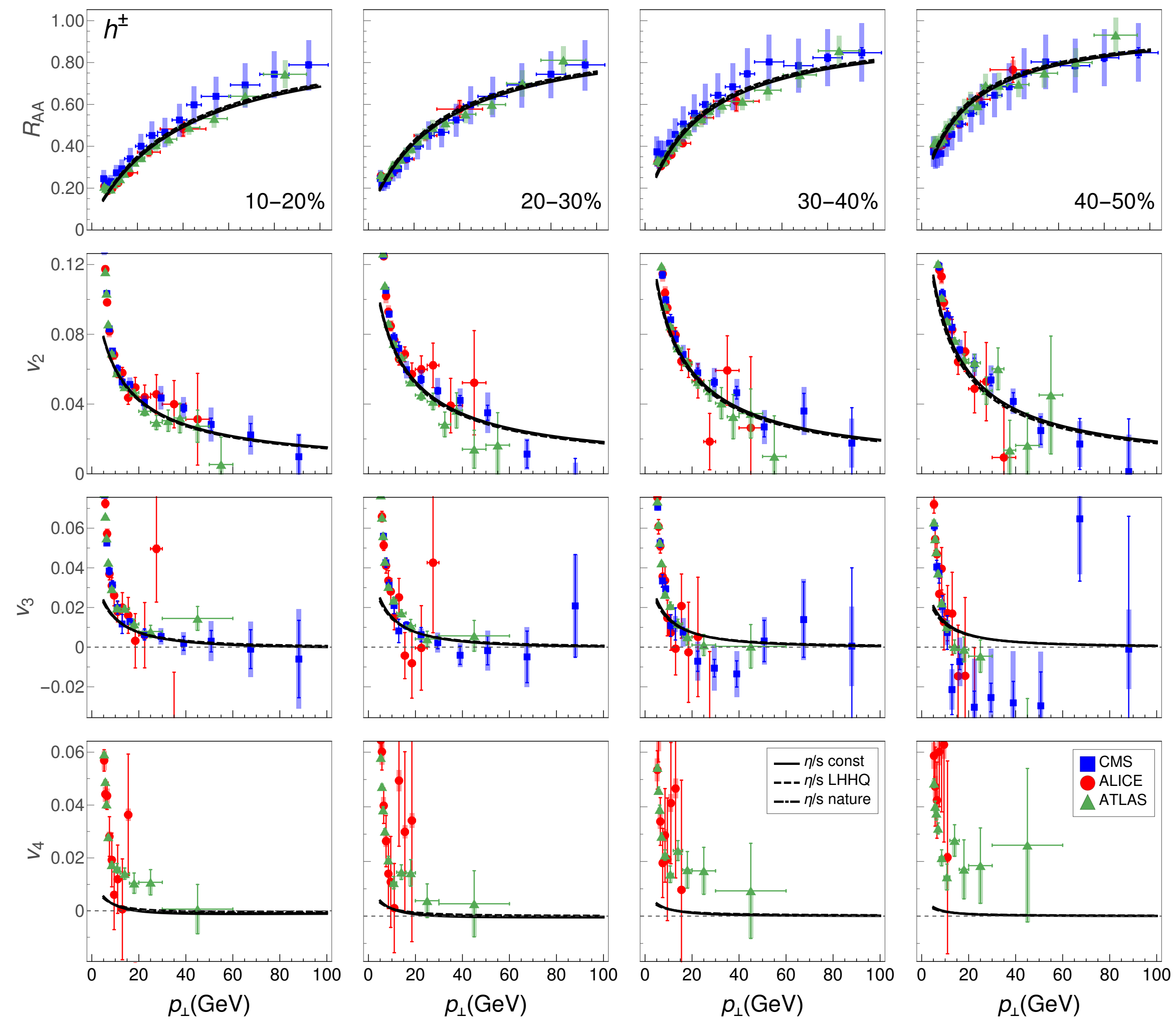


- Pion, kaon, proton multiplicities and  $v_2\{4\}$  are reproduced by varying the TRENTo normalization factor for three  $\eta/s$  parametrizations.



# Results

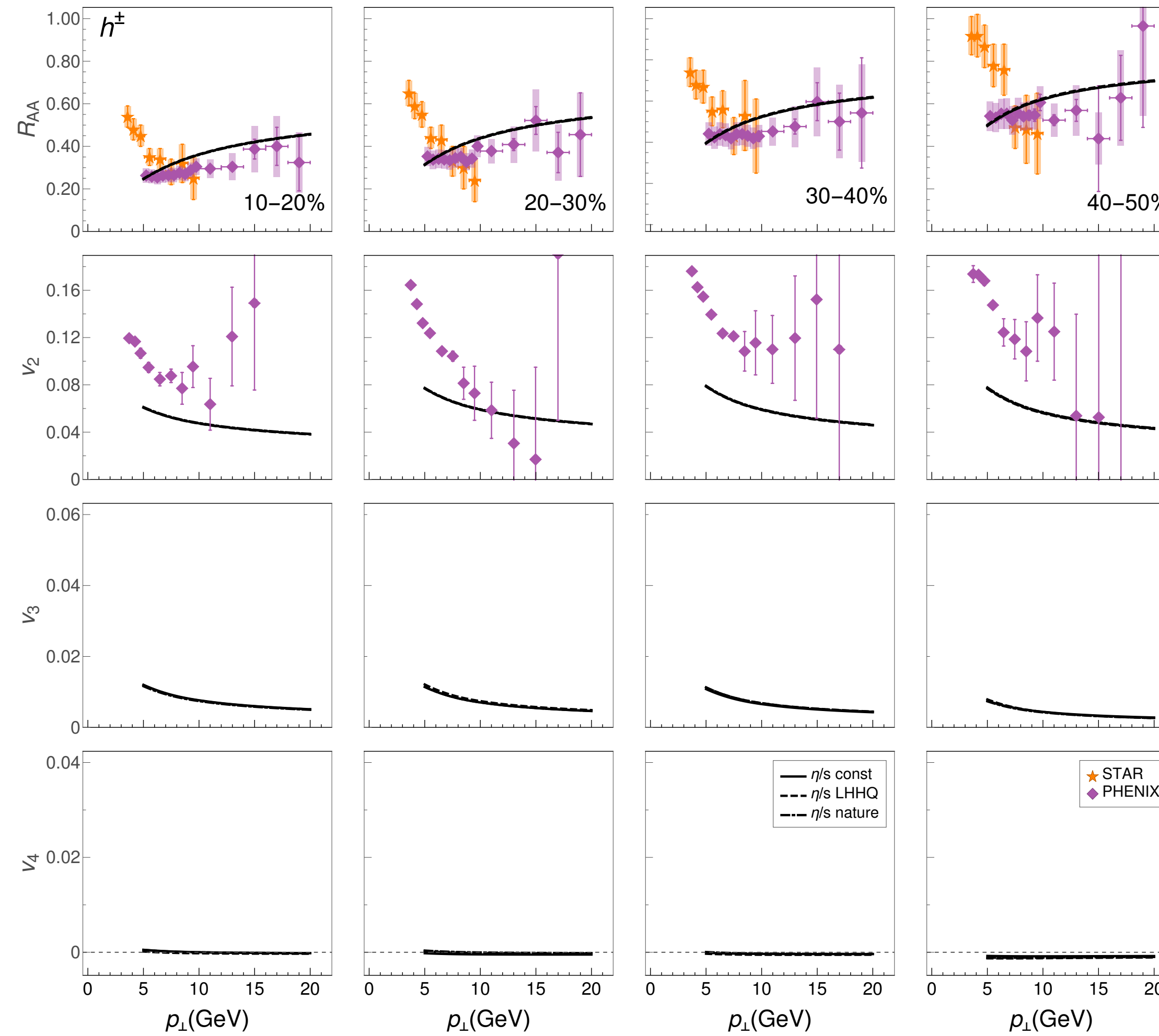
BK, D. Zigic, I. Salom, J. Auvinen, P. Huovinen, M. Djordjevic and M. Djordjevic arXiv:2305.11318



Pb + Pb ( $\sqrt{s} = 5.02$  TeV)

# Results

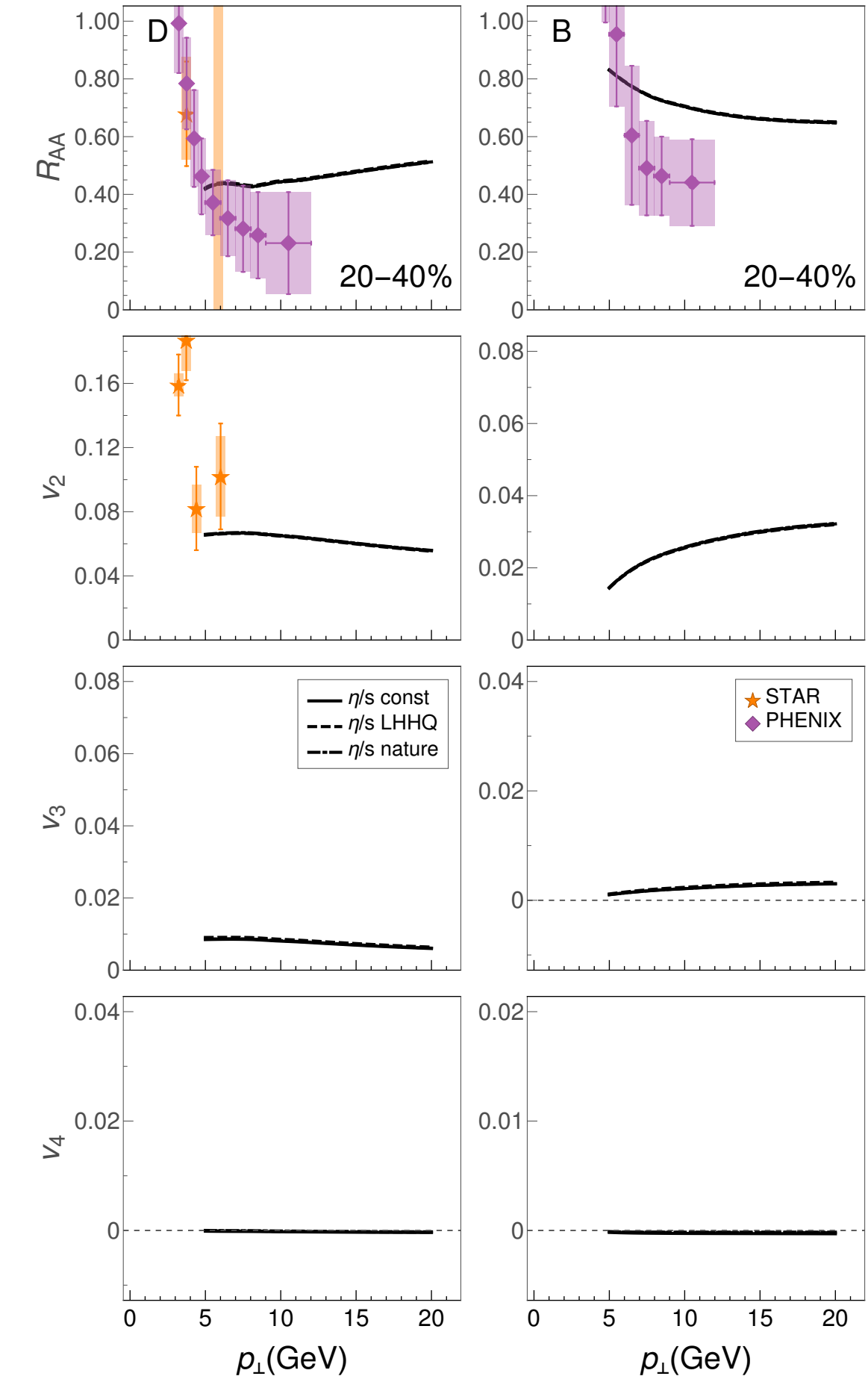
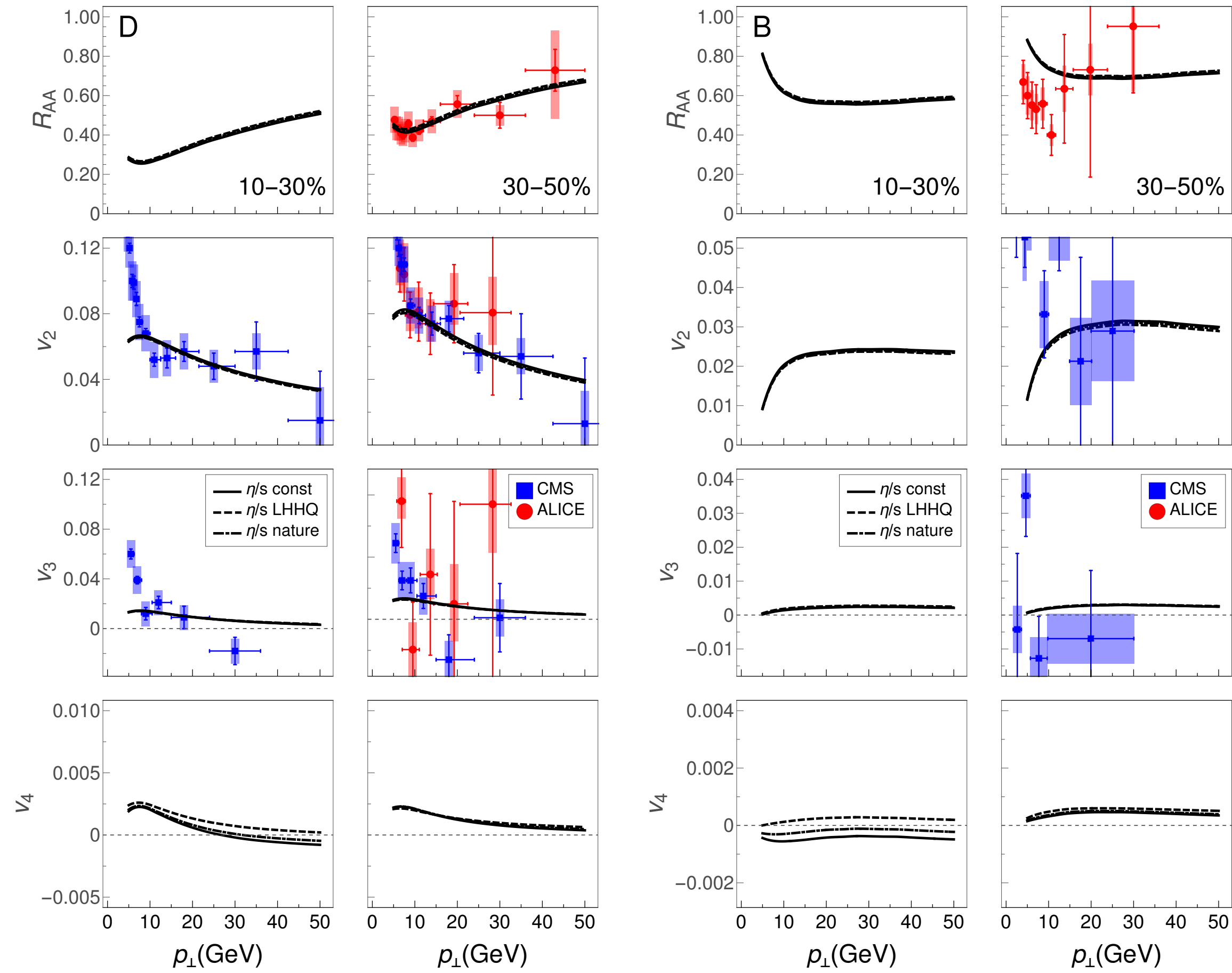
BK, D. Zigic, I. Salom, J. Auvinen, P. Huovinen, M. Djordjevic and M. Djordjevic arXiv:2305.11318



Au + Au ( $\sqrt{s} = 200$  GeV)

# Results

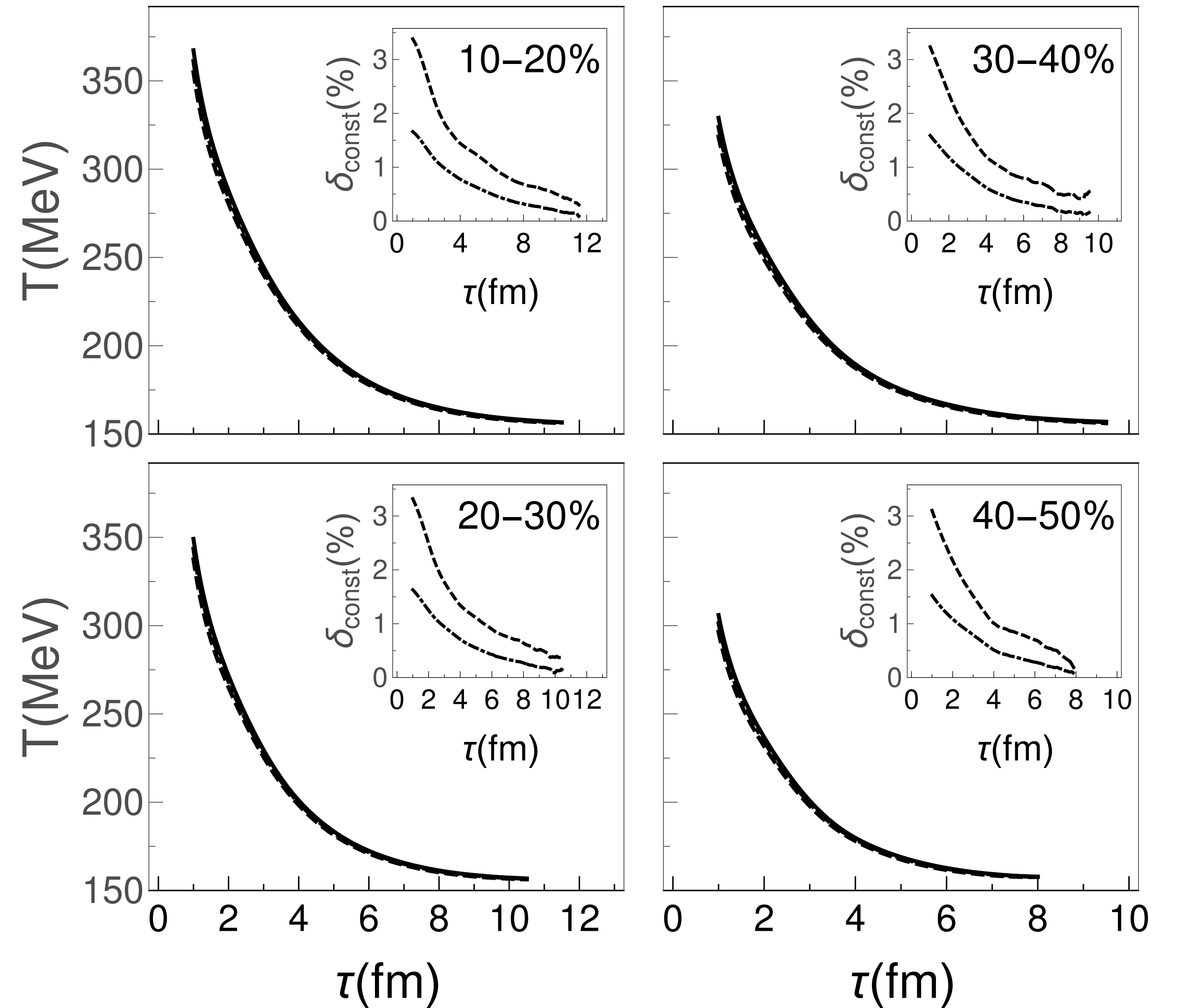
BK, D. Zigic, I. Salom, J. Auvinen, P. Huovinen, M. Djordjevic and M. Djordjevic arXiv:2305.11318



# Average jet perceived temperature

BK, D. Zigic, I. Salom, J. Auvinen, P. Huovinen, M. Djordjevic and M. Djordjevic arXiv:2305.11318

- Pb + Pb  $s = 5.02$  TeV
- Full = LHHQ; DotDashed = Nature,  
Dashed = Constant
- Inset: Dotdashed = Nature,  
Dashed = LHHQ
- Temperature difference during evolution  
is very small.
- Insufficient to lead to observable difference  
in the results.



# Theoretical approach :

## Transport coefficient from dynamical energy loss formalism

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- Transport coefficient ( $\hat{q}$ )  $\equiv$  Squared average transverse momentum exchange between the medium and the fast parton per unit length
- Interaction between the parton and medium is characterized by the HTL resummed elastic collision rate:

$$\frac{d\Gamma_{el}}{d^2q} = 4C_A \left[ 1 + \frac{n_f}{6} T^3 \frac{\alpha_s^2}{q^2 q^2 + \mu_E^2} \right]$$

- After including running coupling and finite magnetic mass:

$$\frac{d\Gamma_{el}}{d^2q} = \frac{C_A}{\pi} T \alpha(ET) \frac{\mu_E^2 - \mu_M^2}{(q^2 + \mu_E^2)(q^2 + \mu_M^2)}$$

- In fluid rest frame:

$$\hat{q} = \int_0^{6ET} d^2q q^2 \cdot \frac{d\Gamma_{el}}{d^2q} = C_A T \frac{4\pi}{(11 - \frac{2}{3}n_f)} \frac{\mu_E^2 \ln \frac{6ET + \mu_E^2}{\mu_E^2} - \mu_M^2 \ln \frac{6ET + \mu_M^2}{\mu_M^2}}{\ln(\frac{ET}{\Lambda^2})}$$

# $\eta/s$ from the transport coefficient

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- In the limit  $ET \rightarrow \infty$ :

$$\hat{q} = C_A \frac{4\pi}{11 - \frac{2}{3}n_F} \frac{4\pi}{\Lambda} \frac{1 + \frac{n_F}{6}}{W(\xi(T))} (1 - x_{ME}^2) T^3$$

- $\xi(T) = \frac{1 + \frac{n_f}{6}}{11 - \frac{2}{3}n_f} \frac{4\pi T^2}{\Lambda}$ ,  $W \equiv$  Lambert's  $W$  function,  $x_{ME} = \mu_M/\mu_E$

- $\hat{q}$  is weakly dependent on jet energy  $E$ .
- In weakly coupled limit:

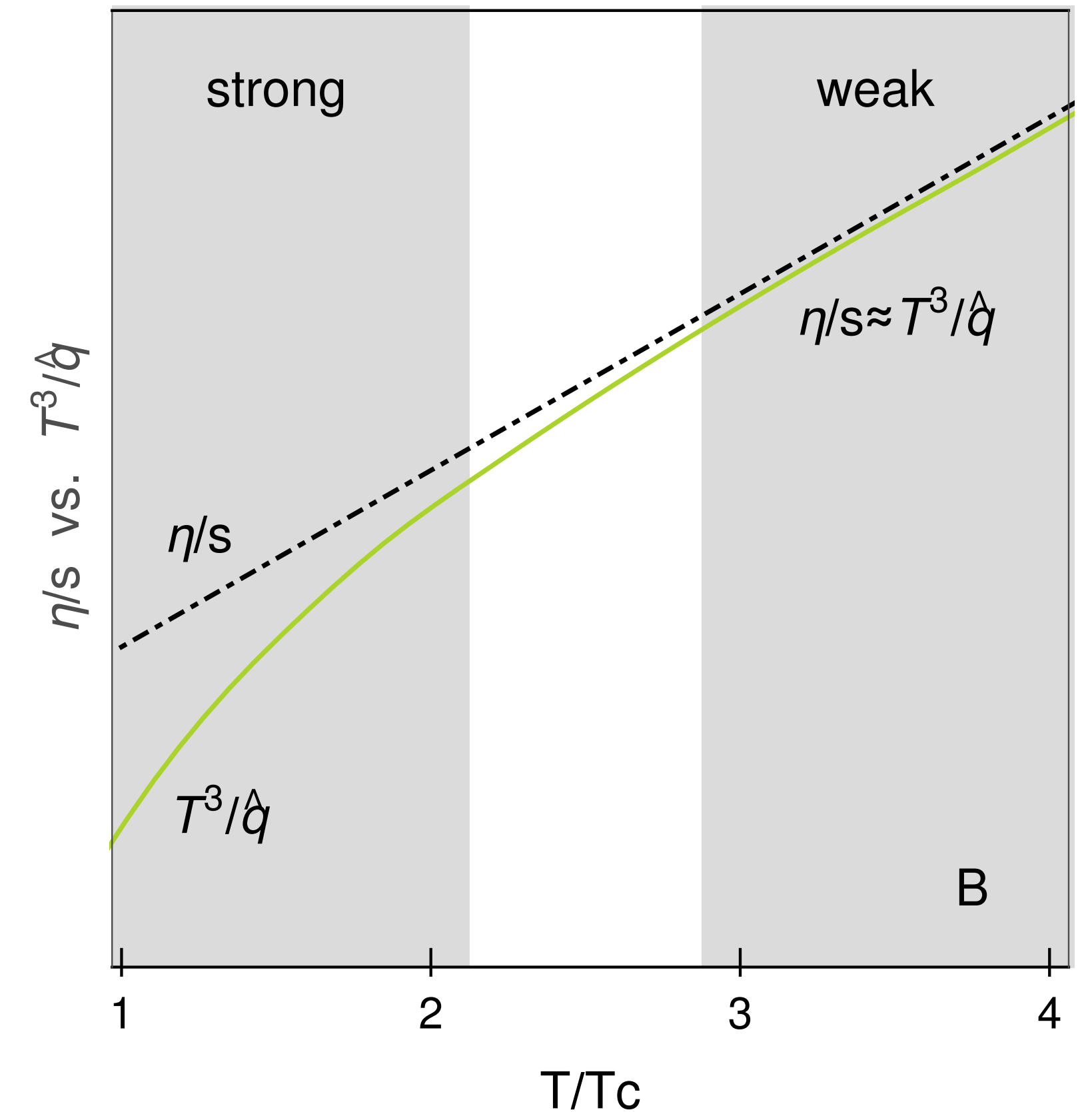
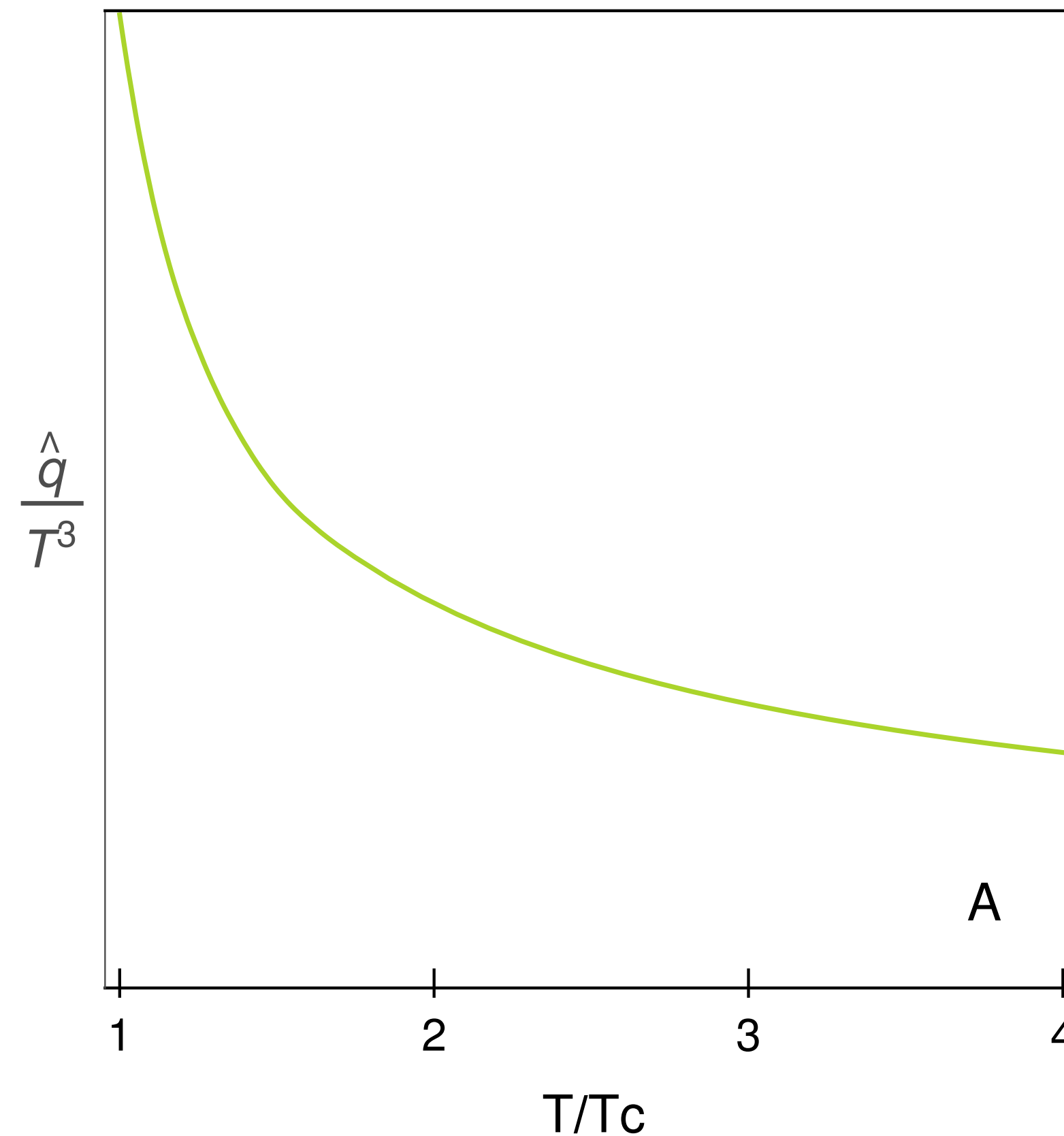
$$\eta/s \approx 1.25 T^3 / \hat{q}$$

Phys. Rev. Lett. 99 192301 (2007), Phys. Rev. D 104, L071501 (2021)

# $\eta/s$ from the transport coefficient

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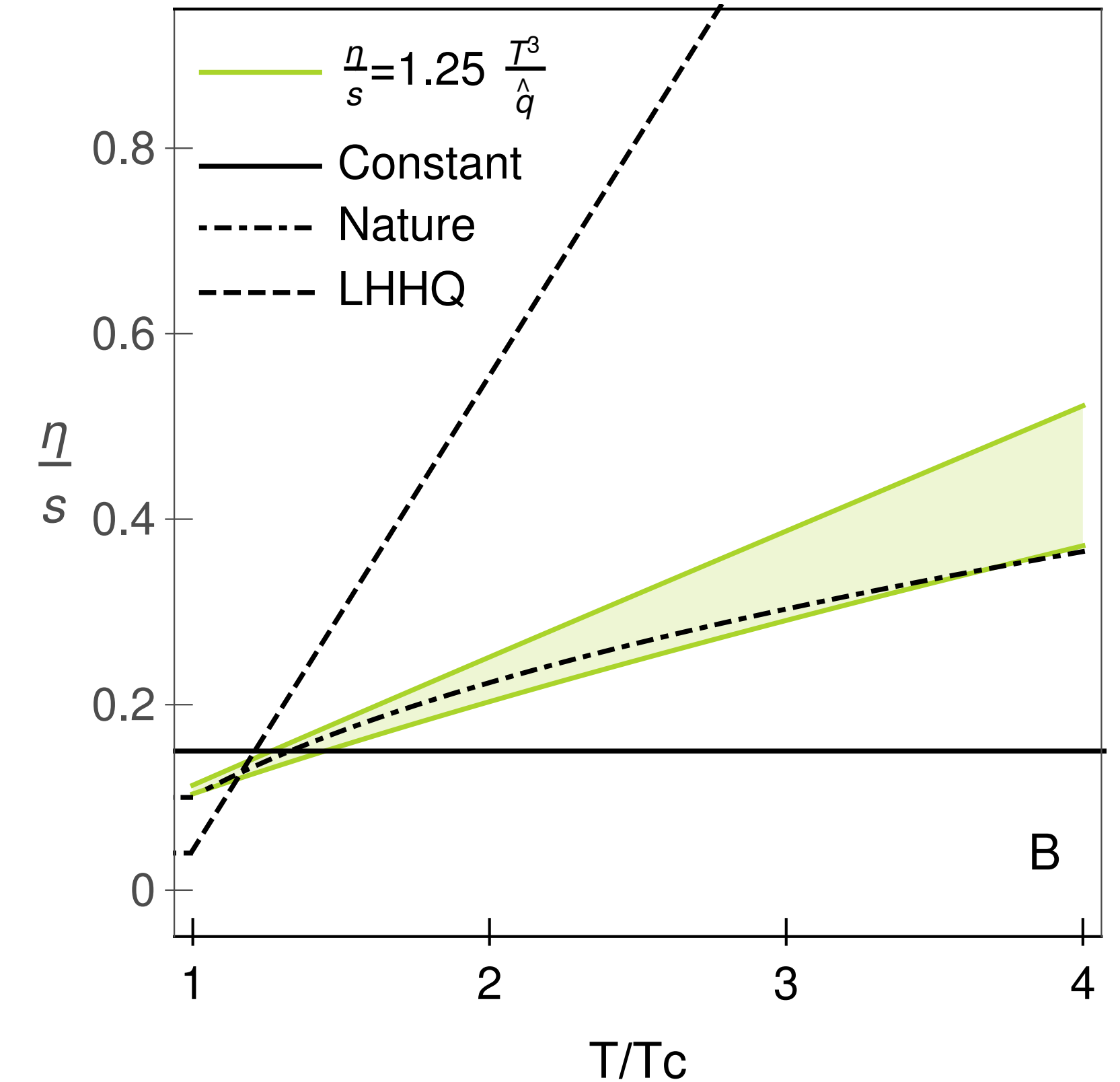
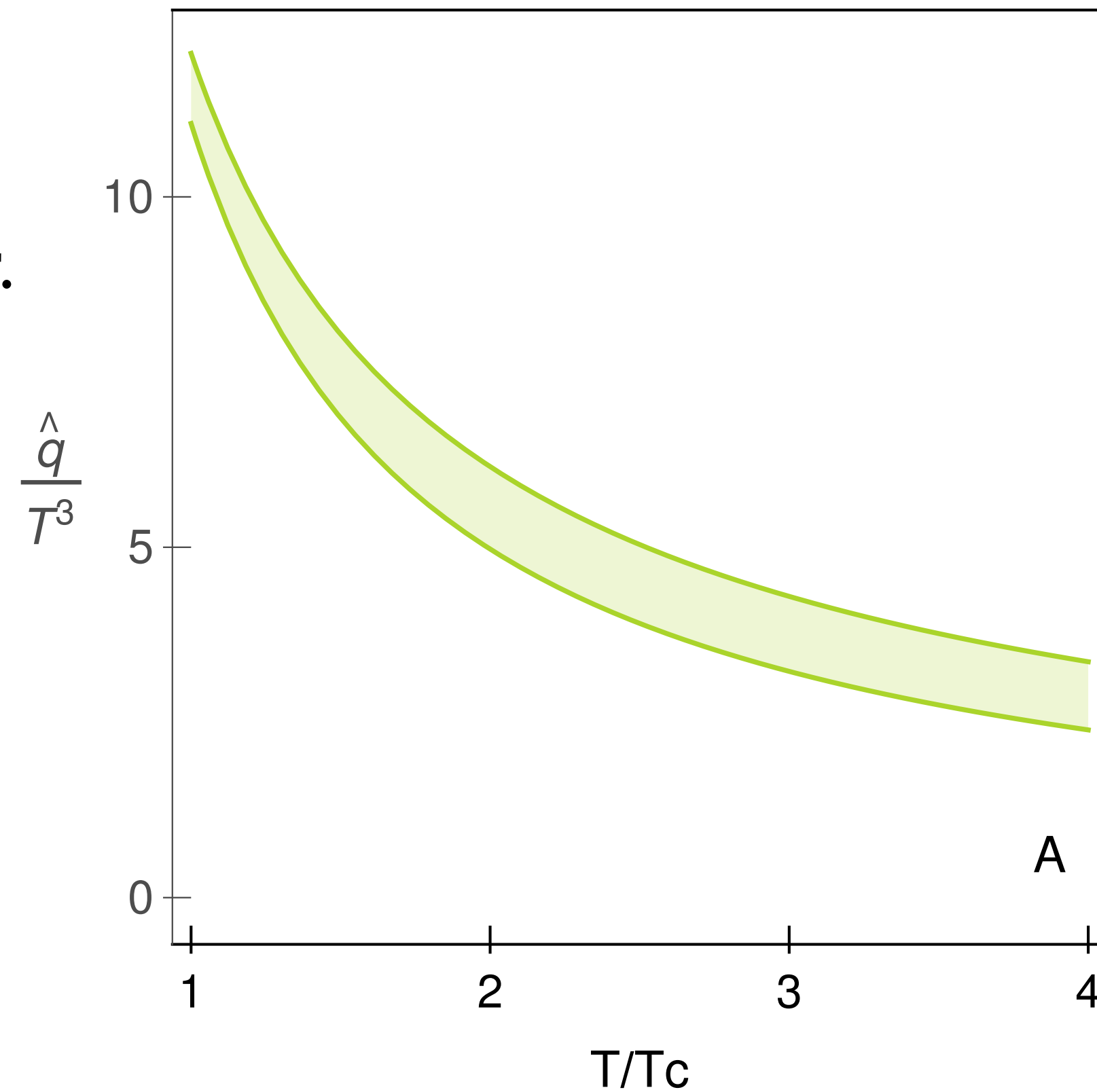
- $\hat{q}$  quantifies the parton coupling strength in the medium
- $\hat{q}/T^3$  must rise rapidly near  $T_c$  from above.
- Our formalism valid in weakly coupled regime.
- $T^3/\hat{q}$  and  $\eta/s$  should agree in the weak coupling regime.
- Soft-to-hard boundary



# $\eta/s$ from the transport coefficient

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- $\hat{q}/T^3$  shows expected behavior.
- Enhanced quenching near  $T_c$ .
- $\eta/s$  is surprisingly close to the constraints from Bayesian analysis.





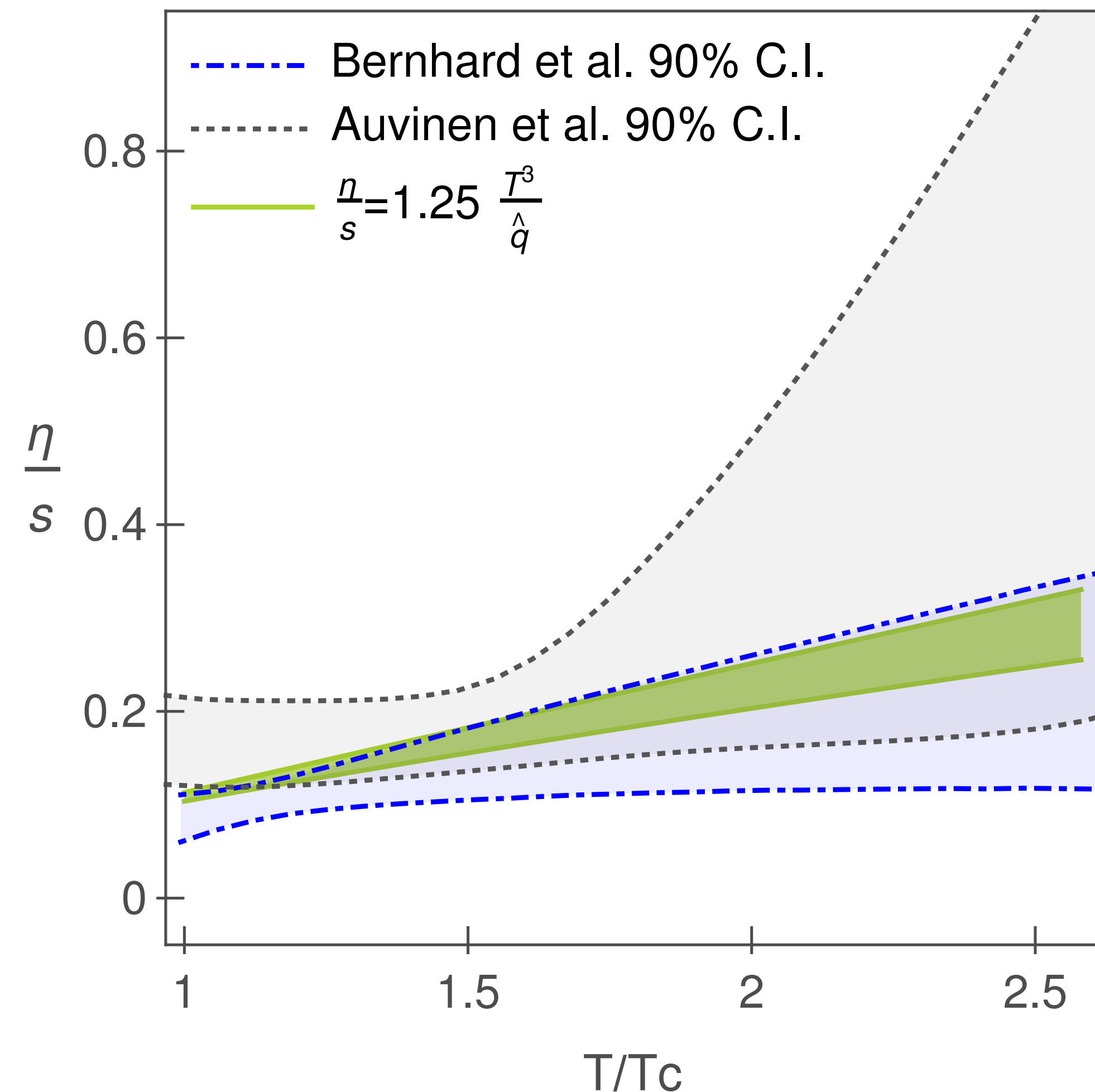
# $\eta/s$ from the transport coefficient

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- Uncertainty due to initial jet energy is very small
- Surprisingly close to the parametrization inspired by the Bayesian analysis.
- Does not drop significantly below the inferred  $\eta/s$  values near  $T_c$ .
- No soft-to-hard boundary.

Blue → Nature Phys. 15, no. 11, 1113-1117 (2019)

Black → Phys. Rev. C 102, 044911 (2020)



# Conclusion

- We use generalized DREENA-A to compute high- $p_{\perp}$  energy loss.
- In the phenomenological approach:
  - Three different  $(\eta/s)(T)$  parametrizations have been considered.
  - The predictions from the generalized DREENA-A for three  $\eta/s$  scenarios lead to plots that are almost indistinguishable.
  - The difference in the average jet-perceived temperature for the three cases is less than 2%.
  - High- $p_{\perp}$  observables are not sensitive to such small temperature difference.
- In the theoretical approach:
  - Transport coefficient and jet quenching strength are calculated from the dynamical energy loss formalism.
  - $\eta/s$  shows surprisingly good agreement all the way to  $T_c$  with constraints extracted from existing Bayesian analyses. Provides much smaller uncertainties at high temperature.
  - Intriguing hypothesis: quasiparticle picture is consistent at the entire temperature range.
  - No guidance on locating soft-to-hard boundary.

**Thank you for your attention**

- Mass of light quark  $M = \mu_E/6$
- Mass of charm and bottom quark 1.2 GeV and 4.75 GeV
- Gluon mass  $m_g = \mu_E/2$
- $\mu_M/\mu_E = 0.6$
- $\Lambda_{QCD} = 0.2\text{GeV}$
- Constant  $\eta/s$  (0.15 for Pb+Pb and 0.12 for Au+Au collision)
- Nature:  $(\eta/s)_{\min} = 0.1, (\eta/s)_{\text{slope}} = 1.11, (\eta/s)_{\text{crv}} = -0.48$
- LHHQ:  $(\eta/s)_{\min} = 0.04, (\eta/s)_{\text{slope}} = 3.30, (\eta/s)_{\text{crv}} = 0$

# Modeling the bulk evolution

- Particlization is performed using Cooper-Frye prescription at isothermal space time hypersurface at 151 MeV.
- UrQMD is used to simulate microscopic dynamics of hadronic system.
- Bulk viscosity parametrized as

$$(\zeta/s)(T) = \frac{(\zeta/s)_{\max}}{1 + \frac{T - T_0}{(\zeta/s)_{\text{width}}}}^2$$

with  $(\zeta/s)_{\max} = 0.03$ ,  $(\zeta/s)_{\text{width}} = 0.022$  and  $T_0 = 0.183 \text{ GeV}$ .

- We use lattice QCD based EoS from HotQCD (high temperature) + HRG (low temperature) EoS.